

Multiscale computational modeling of heterogeneous gas-solid reactions of the direction reduction process of iron ores

Patrícia Metolina
André Luiz Nunis da Silva
Anthony G. Dixon
Roberto Guardani

Palestra apresentada no SEMINÁRIO DE REDUÇÃO DE MINÉRIOS E MATÉRIAS-PRIMAS, 51., 2023, São Paulo. 30 slides

A série “Comunicação Técnica” compreende trabalhos elaborados por técnicos do IPT, apresentados em eventos, publicados em revistas especializadas ou quando seu conteúdo apresentar relevância pública. REPRODUÇÃO PORIBIDA

MULTISCALE COMPUTATIONAL MODELING OF HETEROGENEOUS NON-CATALYTIC GAS-SOLID REACTIONS OF THE DIRECT REDUCTION PROCESS OF IRON ORE

Patrícia Metolina – Escola Politécnica da Universidade de São Paulo / Instituto de Pesquisas Tecnológicas / Worcester Polytechnic Institute

André Luiz Nunis da Silva – Instituto de Pesquisas Tecnológicas

Anthony G. Dixon – Worcester Polytechnic Institute

Roberto Guardani – Escola Politécnica da Universidade de São Paulo

Agosto 2023

Contents

01. Introduction

02. Literature Review

03. Objectives

04. Methodology

05. Results and Discussion

06. Conclusion



Contents

01. Introduction

02. Literature Review

03. Objectives

04. Methodology

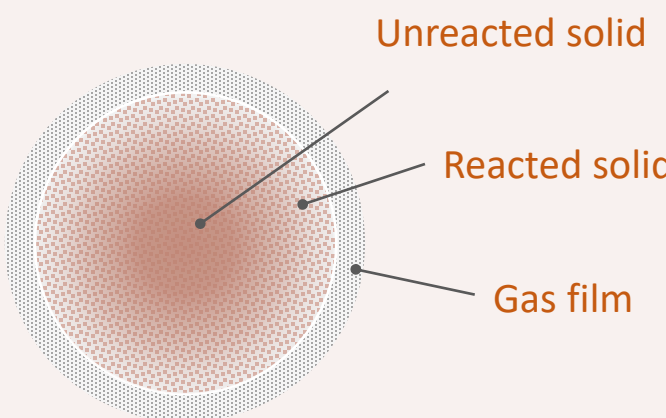
05. Results and Discussion

06. Conclusion



INTRODUCTION

Importance of multiscale modeling



Unreacted solid

Reacted solid

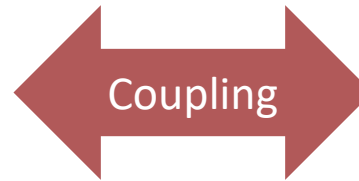
Gas film

Particle (inside modeling)

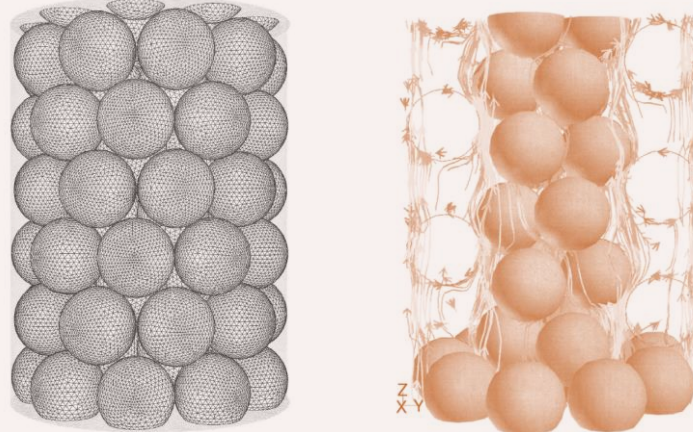
- ✓ Mass and heat transport mechanisms
- ✓ Structural changes over time
- ✓ Physical properties of the systems changes

Non-catalytic gas-solid

reactions



**Multi-scale
approach**



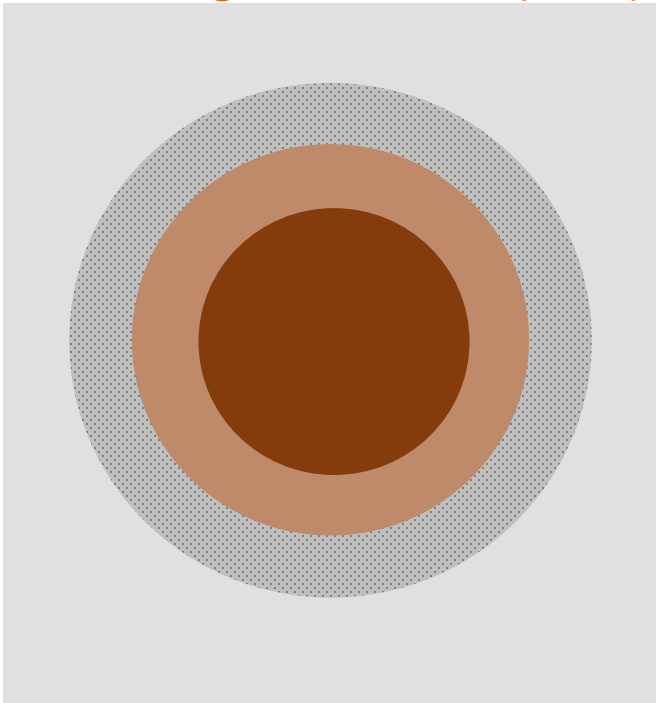
Moving - Bed

- ✓ Mass and heat transport mechanism
- ✓ Fluid flow between particles
- ✓ Random arrangement of particles

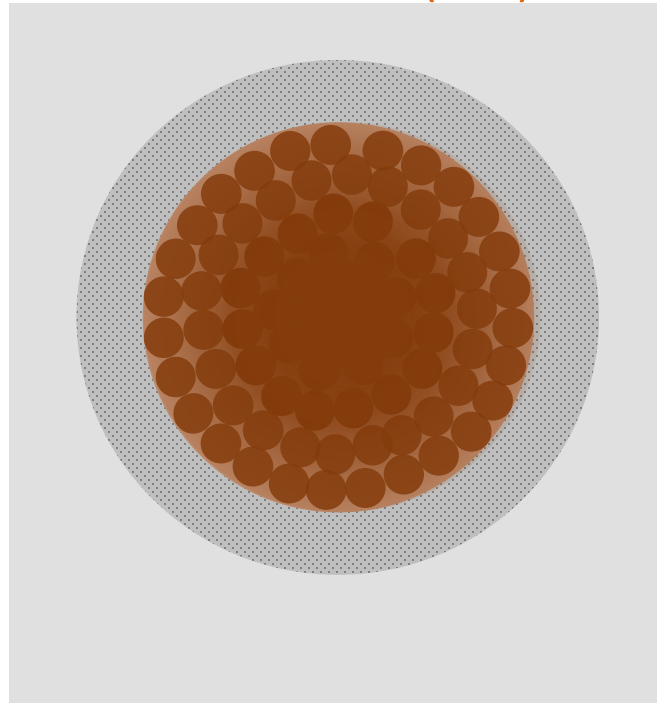
INTRODUCTION

Non-catalytic gas-solid reactions models

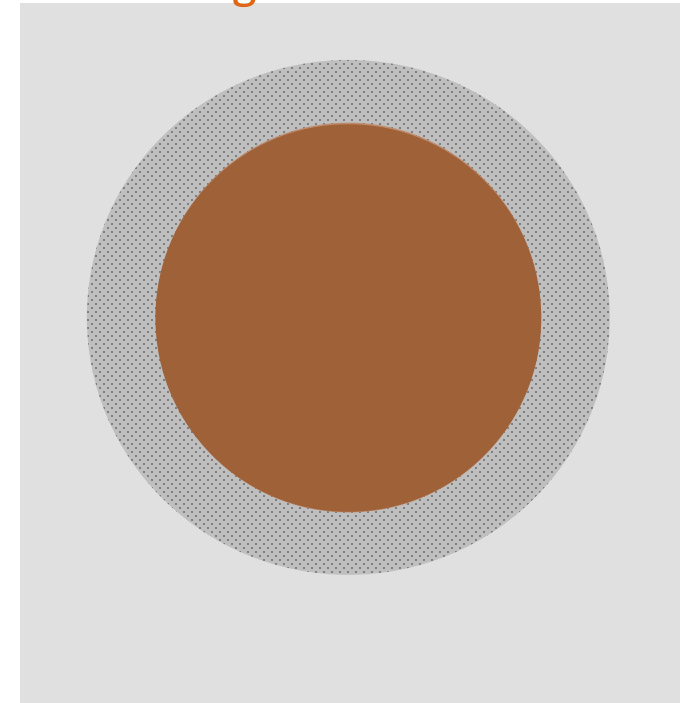
Shrinking Core Model (SCM)



Grain Model (GM)



Homogeneous Model



Heterogeneous



Homogeneous

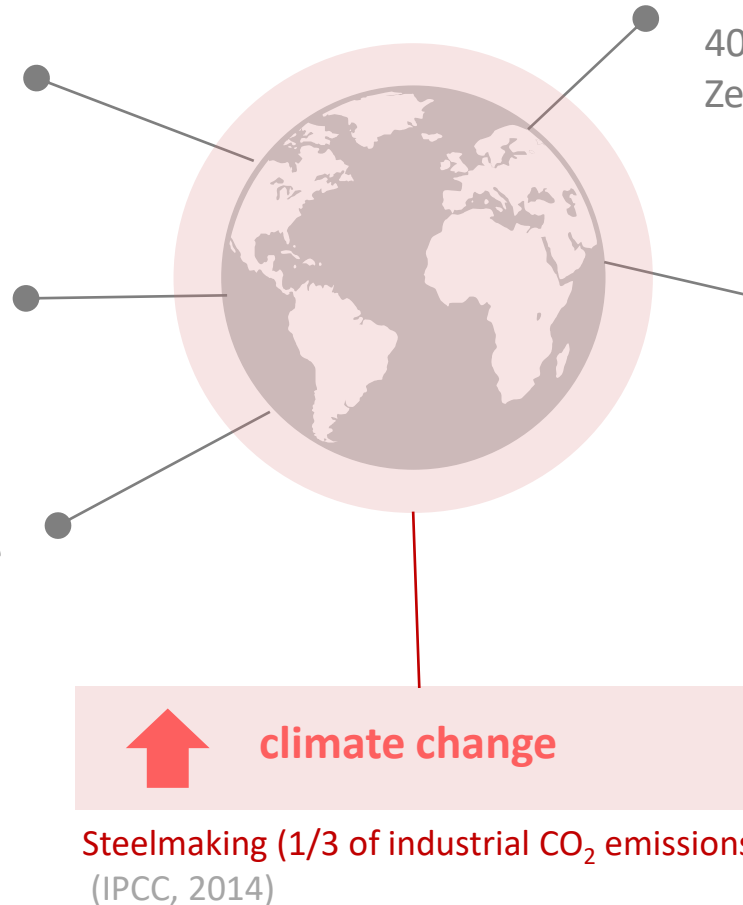
INTRODUCTION

Direct Reduction Of Iron Ore (DRI)

~110 million tons of iron
is the annual world production
(MIDREX, 2022)

High energy consumption
is decreased compared to blast furnace
(IEAGHG, 2018)

Smaller units are more flexible
(Béchara et al., 2018)



Reduction in CO₂ emissions
40 to 50% compared to blast furnace (IEAGHG, 2018)
Zero emission using only H₂

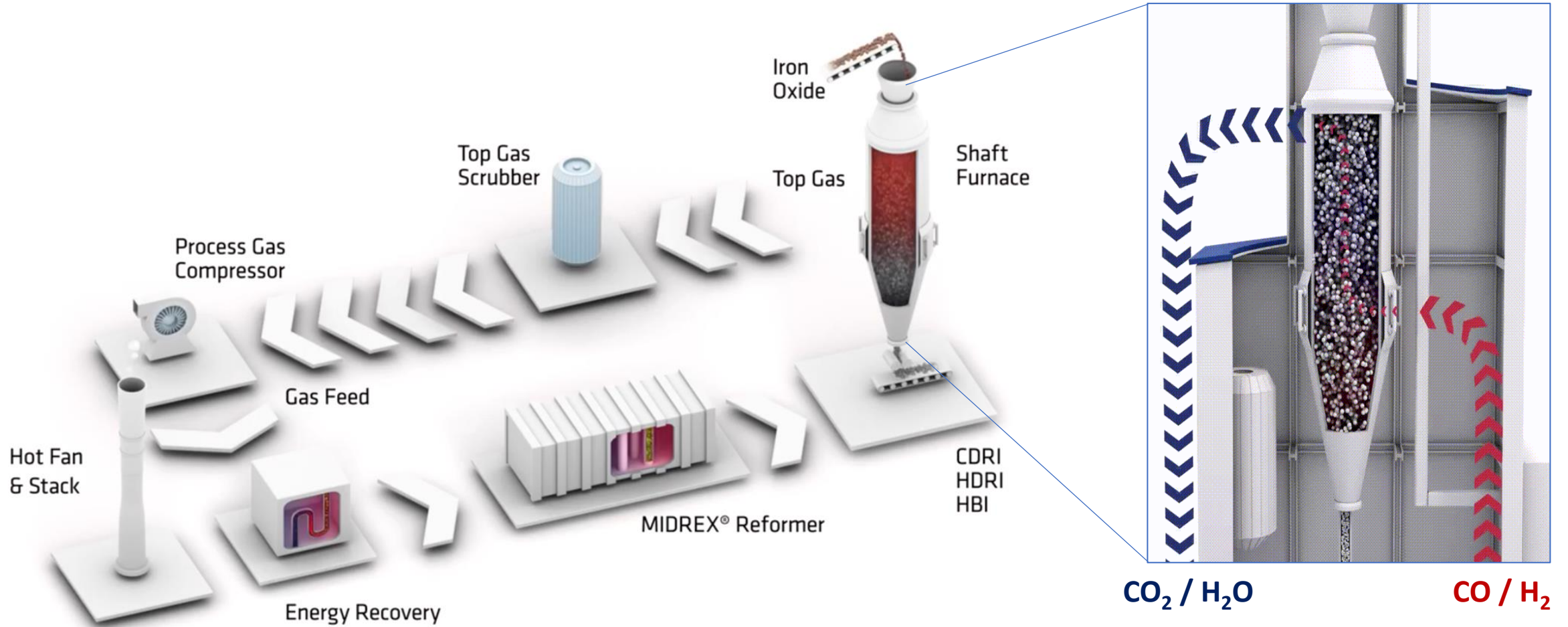
Substitution **for green H₂**
via electrolysis
(Patisson and Mirgaux, 2020)

Paris Agreement
European Green Deal

- Limit global warming to 1.5 °C by 2050
- 55% in CO₂ emission until 2030 and carbon neutrality by 2050

INTRODUCTION

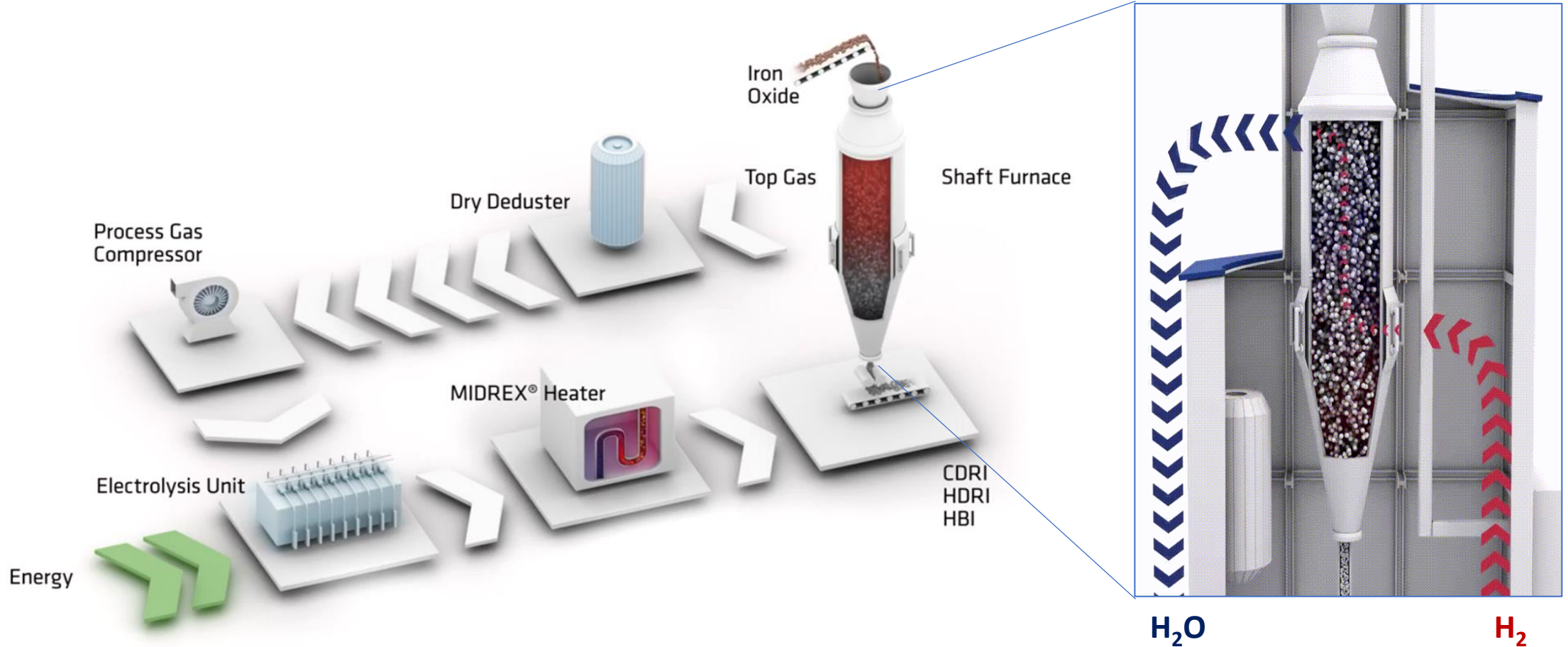
MIDREX Process: Direct Reduction of Iron Ore



MIDREX (2021)

INTRODUCTION

H-DR Process: Hydrogen Direct Reduction of Iron Ore



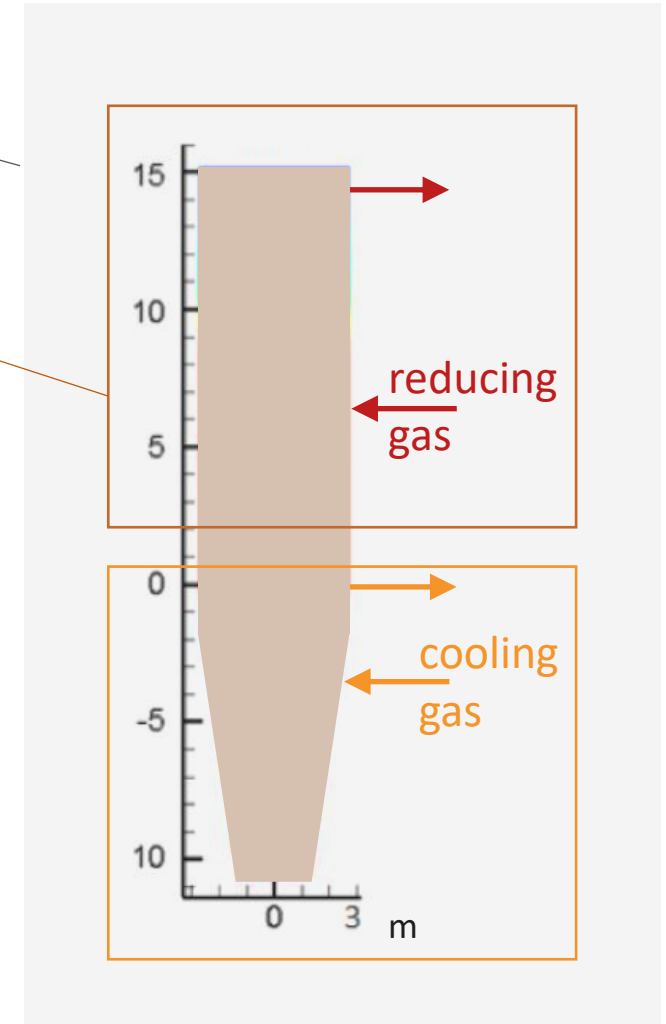
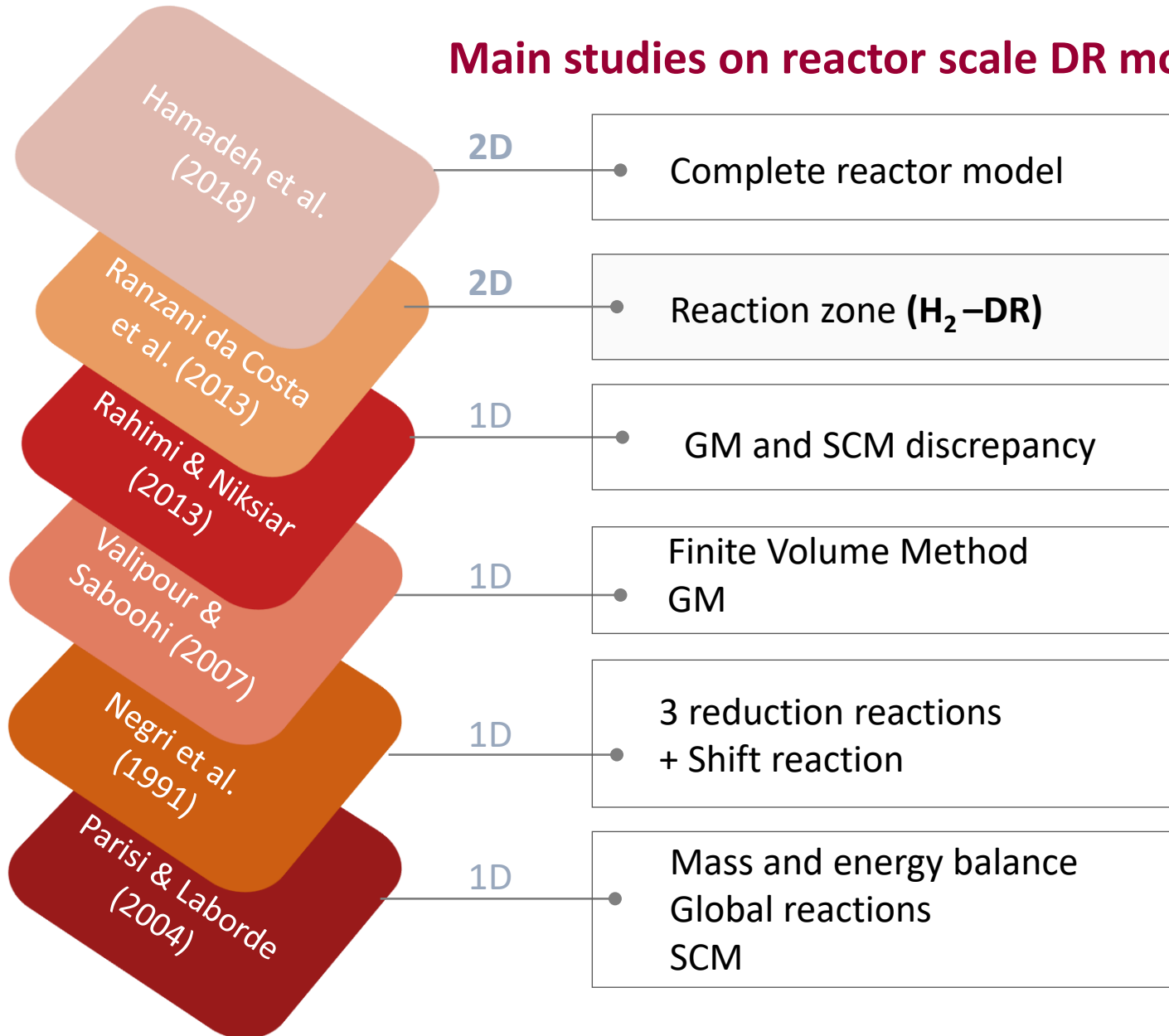
MIDREX (2021)

Contents

01. Introduction
02. Literature Review
03. Objectives
04. Methodology
05. Results and Discussion
06. Conclusion



Main studies on reactor scale DR modeling



Contents

01. Introduction

02. Literature Review

03. Objectives

04. Methodology

05. Results and Discussion

06. Conclusion



OBJECTIVES

Develop a multiscale mathematical model to represent non-catalytic gas-solid reactions applied to the direct reduction of iron ore process

- 1 Explore the influence of the **structural parameters of the pellets** such as size, porosity on **process efficiency**.
- 2 **Validate** the models with experimental data.
- 3 **Predictions** for the hydrogen direct reduction (HDR) process.

Contents

01. Introduction

02. Literature Review

03. Objectives

04. Methodology

05. Results and Discussion

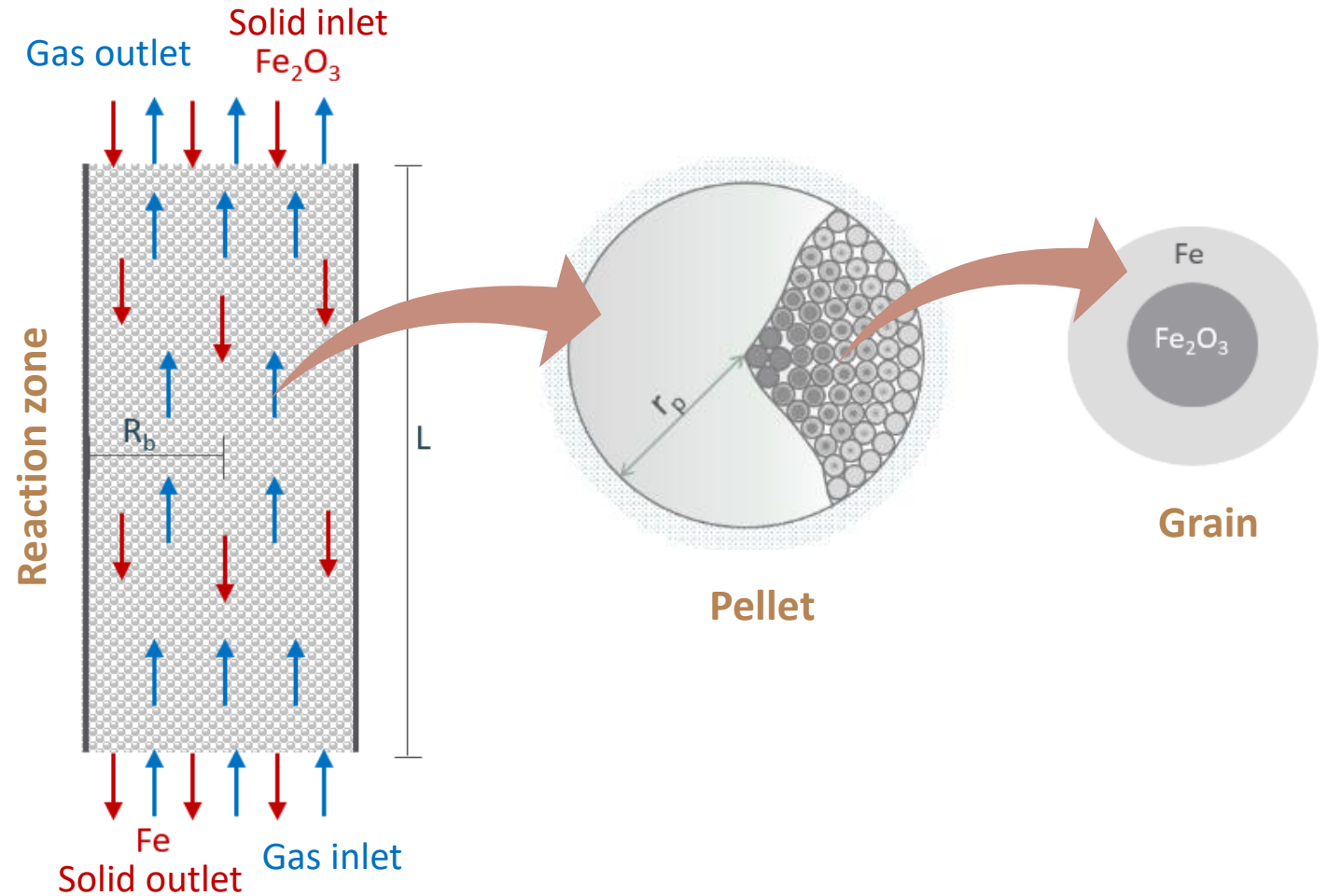
06. Conclusion



Multiscale Modeling

✓ Assumptions:

- Ideal gas mixture
- Plug-flow for both gas and solid
- Ergun equation
- Spherical pellet and grain
- Pellet and grain size constant
- Porosity change
- 2 global reduction reaction



Mathematical Modeling

✓ Finite element method

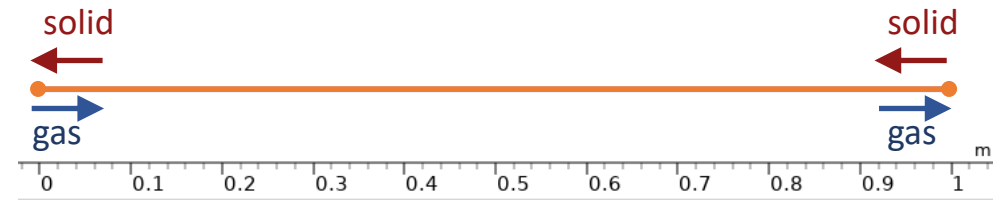
- Comsol Multiphysics 6.0

✓ Reactor-pellet scale coupling

General Extrusion

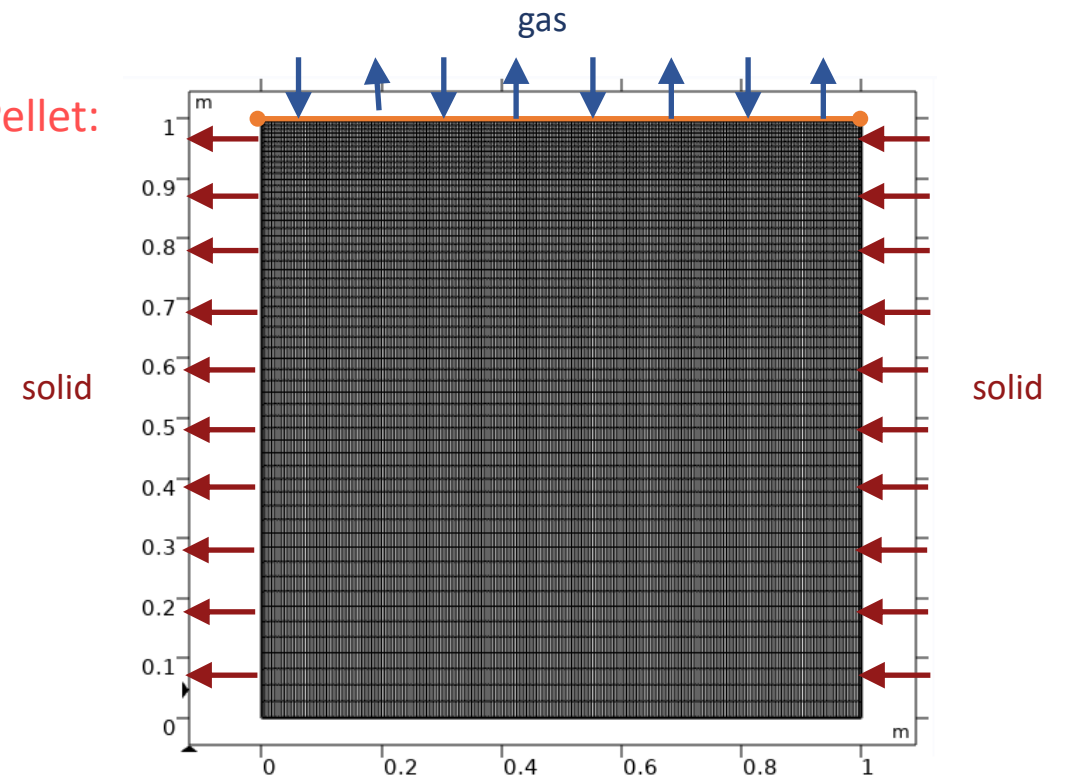
✓ 1D Reactor:

(x axis)



✓ 1D symmetric Pellet:

Extra dimension
(y axis)



Mathematical Modeling

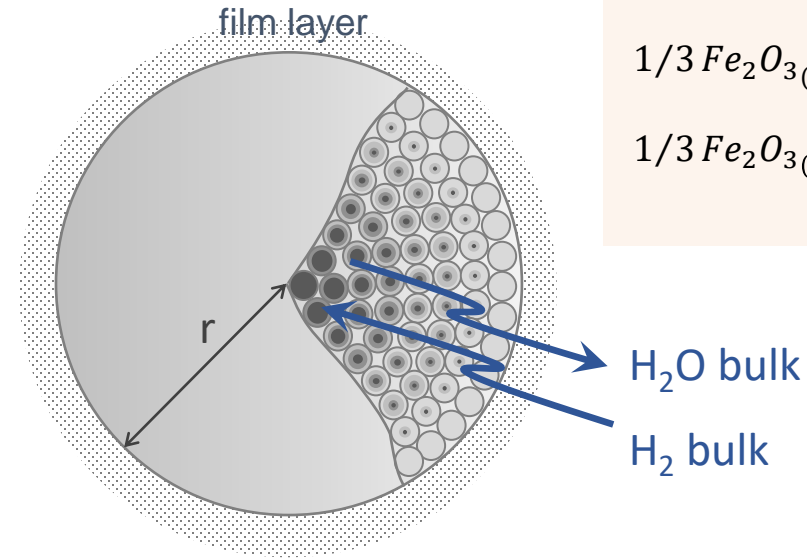
✓ Pellet scale model

- Mass balance for gas ($i = \text{H}_2, \text{H}_2\text{O}, \text{CO}, \text{CO}_2, \text{N}_2$)

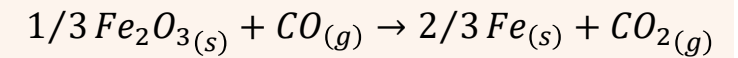
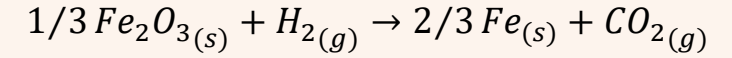
$$-D_{i,eff} \frac{\partial^2 C_i}{\partial r^2} = \frac{2}{r} D_{i,eff} \frac{dC_{p,i}}{dr} + R_i(r, z)$$

- Mass balance for solid ($j = \text{Fe}_2\text{O}_3, \text{Fe}$)

$$u_s \frac{dC_j}{dr} = (1 - \varepsilon_b) R_i(r, z)$$



Reactions



- Kinetic model (Grain model)

$$R_{\text{Fe}_2\text{O}_3} = -\frac{1}{3} A_g k_1 f(x_1) C_{\text{H}_2} - \frac{1}{3} A_g k_2 f(x_1) C_{\text{CO}}$$

$$R_{\text{Fe}} = \frac{2}{3} A_g k_1 f(x_1) C_{\text{H}_2} + \frac{2}{3} A_g k_2 f(x_1) C_{\text{CO}}$$

$$f(x_n) = \left[(1 - x_n)^{-2/3} + \frac{k_n r_g}{D_{effg,i}} (1 - x_n)^{-1/3} - \frac{k_n r_g}{D_{effg,i}} \right]^{-1}$$

Overall conversion of the pellet

$$X_n = \frac{3}{r_p^3} \int_0^{r_p} x_n(r, t) r^2 dr$$

Mathematical Modeling

✓ Moving-bed reactor scale model

- Mass balance for gas ($i = \text{H}_2, \text{H}_2\text{O}, \text{CO}, \text{CO}_2, \text{N}_2$)

$$\frac{d}{dz} \left(-D_i \frac{dC_i}{dz} \right) + u_g \frac{dC_i}{dz} + C_i \left(\frac{u_g P}{T_g} \right) = -(1 - \varepsilon_b) A_p D_{i,eff} \frac{dC_{i,p}}{dr} \Big|_{r=r_p}$$

- Mass balance for solid ($j = \text{Fe}_2\text{O}_3, \text{Fe}$)

$$\frac{dC_j}{dz} = \frac{3}{r_p^3} \int_0^{r_p} C_{j,p} r^2 dr (1 - \varepsilon_b)$$

- Heat balance for gas

$$-\frac{d}{dz} \left(k_{gt} \frac{dT_g}{dz} \right) + \rho_g C_{p,g} u_g \frac{dT_g}{dz} = -(1 - \varepsilon_b) A_p h (T_g - T_s \Big|_{r=r_p})$$

- Heat balance for solid

$$-\frac{d}{dz} \left(k_s \frac{dT_s}{dz} \right) + \rho_s C_{p,eff,p} u_s \frac{dT_s}{dz} = (1 - \varepsilon_b) h \sum R_j (-\Delta H)_j + (1 - \varepsilon_b) A_p h (T_g - T_s)$$

- Ergun equation

$$-\frac{dP}{dz} = \frac{u_g (1 - \varepsilon_b)}{d_p \varepsilon_b^3} \left[\frac{150 \mu (1 - \varepsilon_b)}{d_p} + 1.75 \rho_g u_g \right]$$

where: $\frac{u_g}{u_{feed}} = \frac{P_{feed}}{P} \frac{T_g}{T_{feed}}$

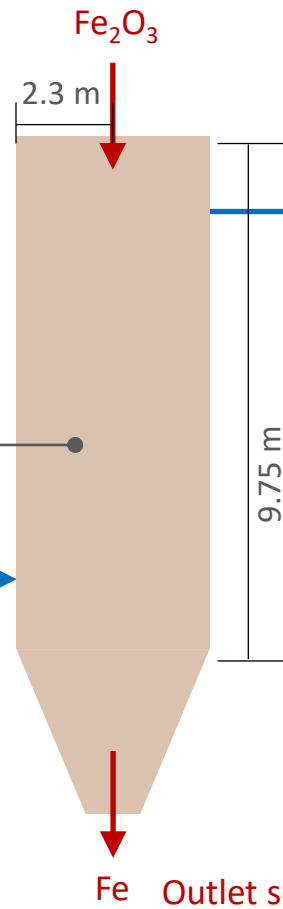
Industrial Plant Data

Gilmore Plant (Parisi and Laborde, 2004)

Inlet solid	
Impurity	4%
Mineral pellet density	4.7 g/cm ³
Pellet diameter	11 mm
Temperature	30 °C
Inlet velocity	3.490E-04 m/s
initial pellet porosity	0.14

Bed properties	
Pellets/volume	0.64 pellet/cm ³
Bed density	2 g/cm ³

Inlet gas	
Flow rate	53863 Nm ³ /h
Pressure	1.4 atm
Temperature	930 °C
Inlet Gas Composition	
H2	52.58%
CO	29.97%
H2O	4.65%
CO2	4.8%
CH4	1.4%
N2	6.6%



Outlet gas	
Pressure	131325 Pa
Temperature	°C
Outlet Gas Composition (dry base)	
H2	37%
CO	18.9%
H2O	21.2%
CO2	14.3%
CH4+N2	8.6%

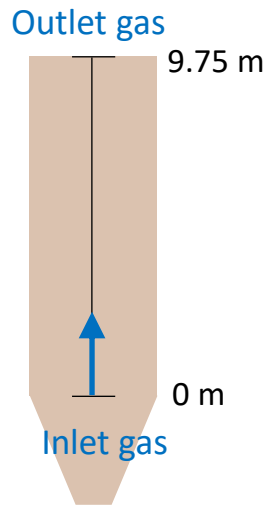
Outlet solid	
Metallization	93%
Mineral pellet density	3.2 g/cm ³
Production	26.4 t/h

Contents

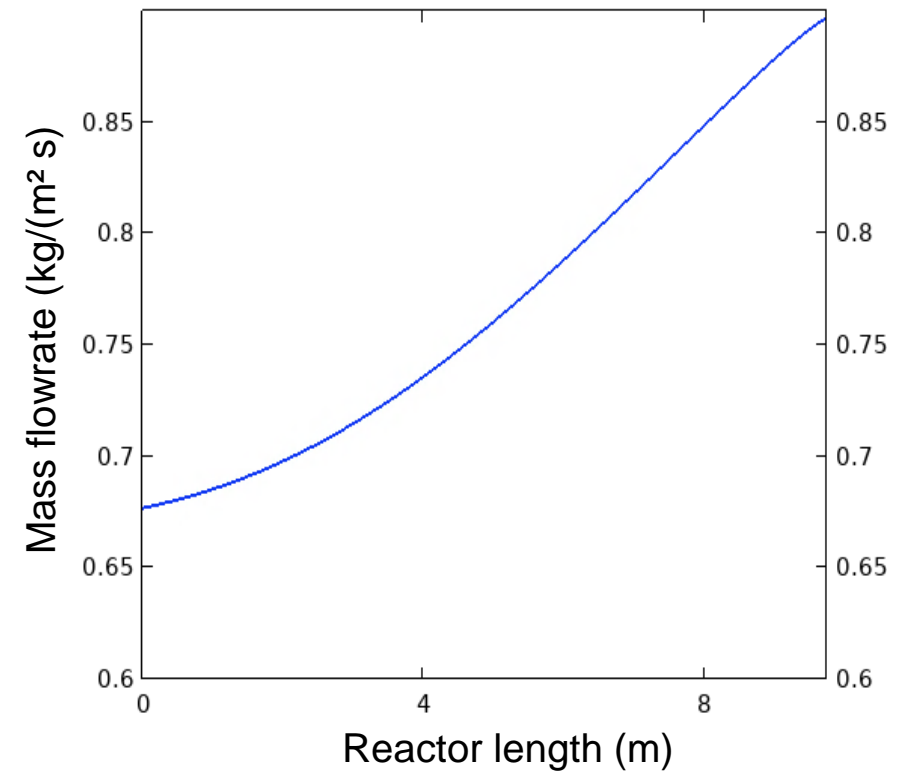
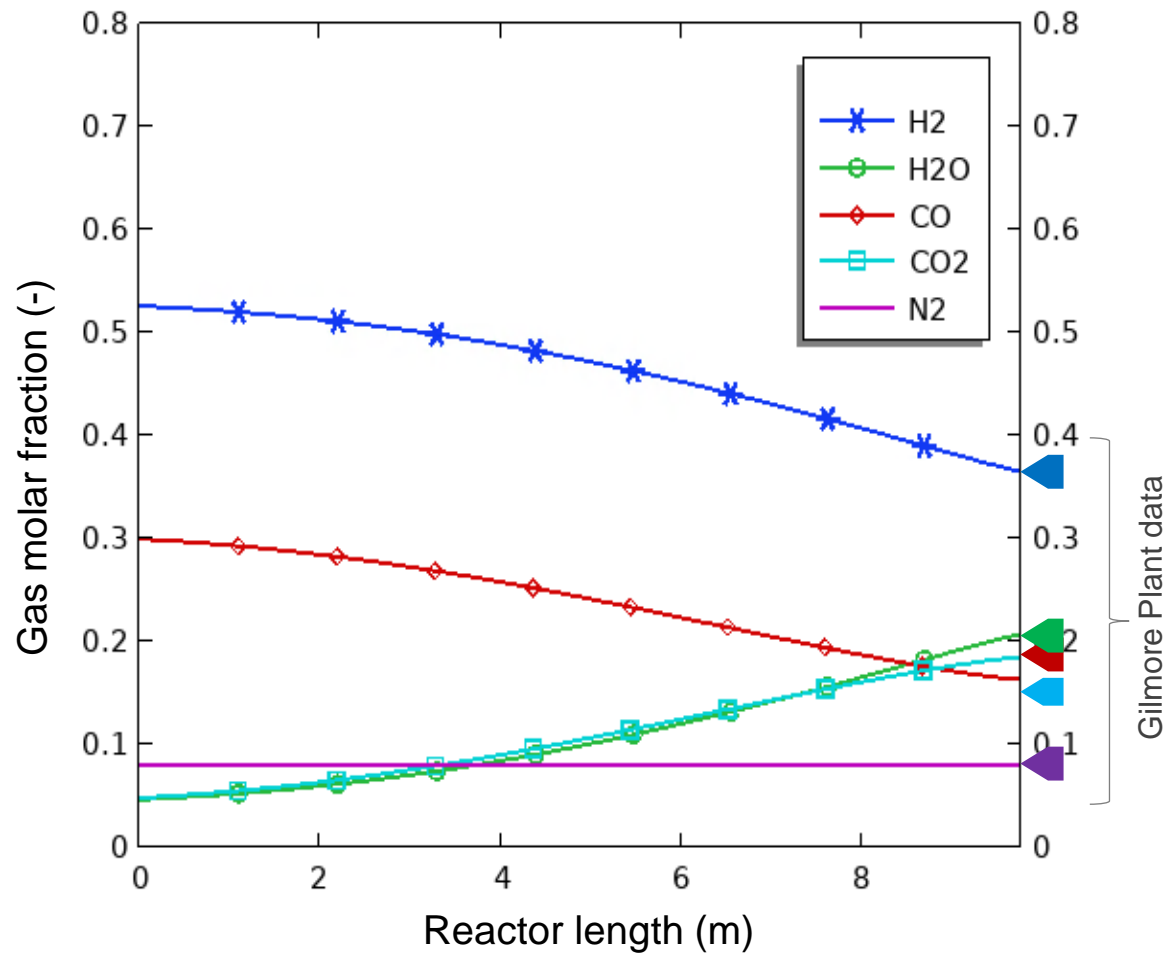
01. Introduction
02. Literature Review
03. Objectives
04. Methodology
05. Results and Discussion
06. Conclusion



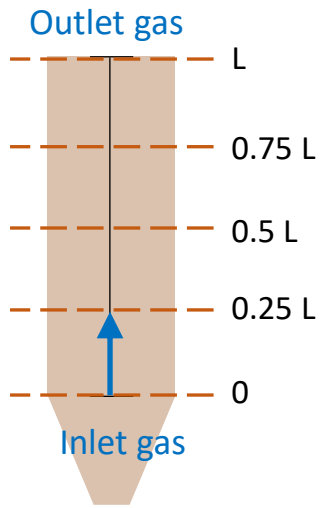
Reactor Scale



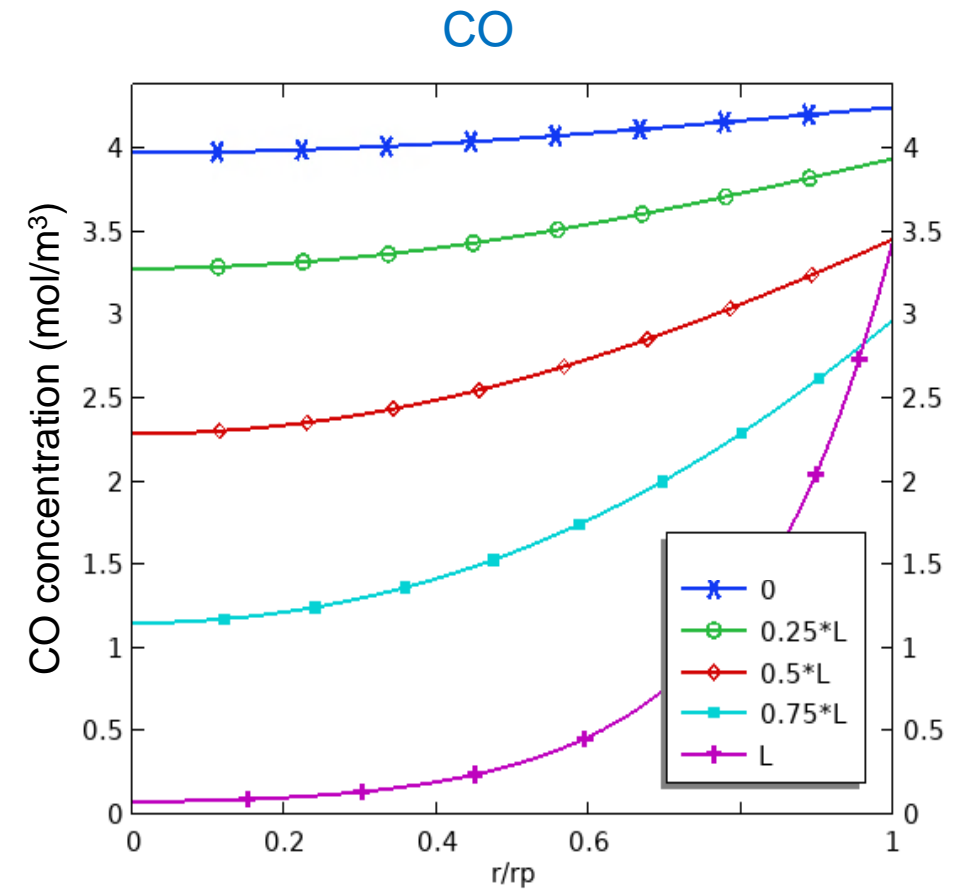
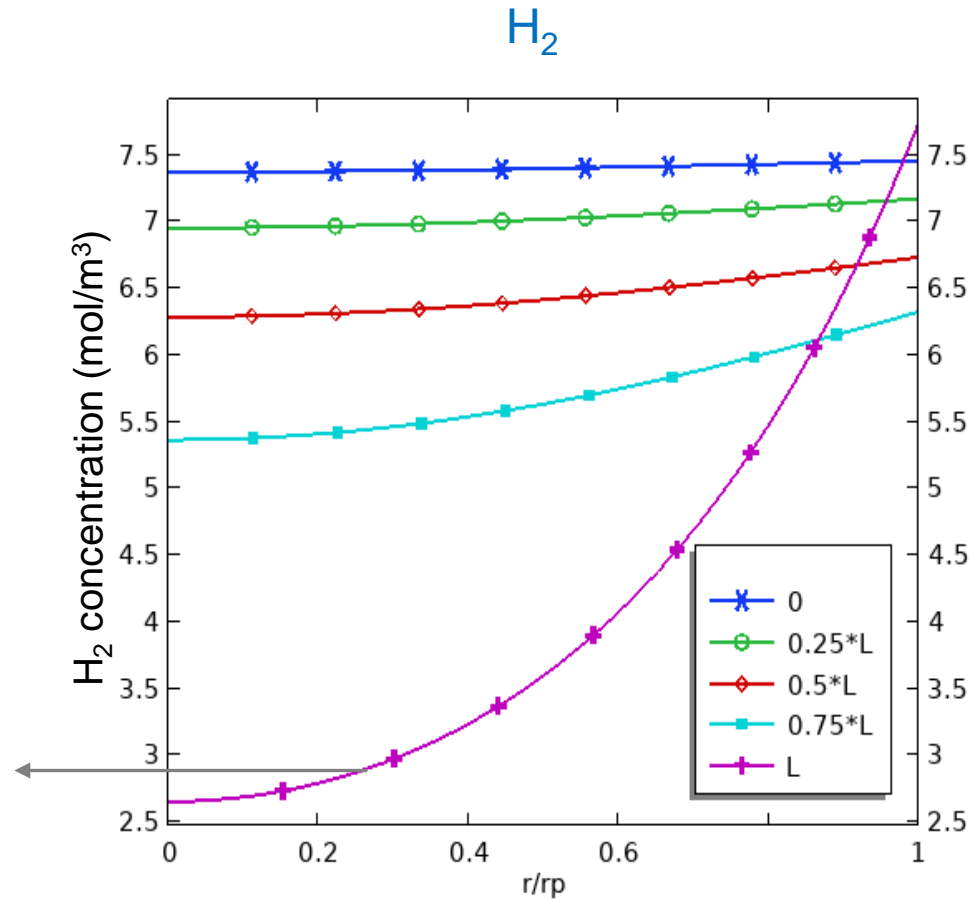
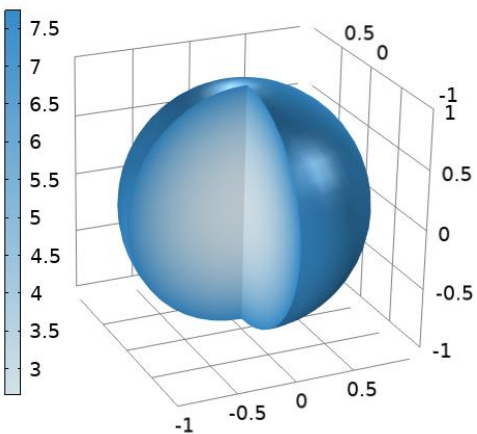
Gas Phase



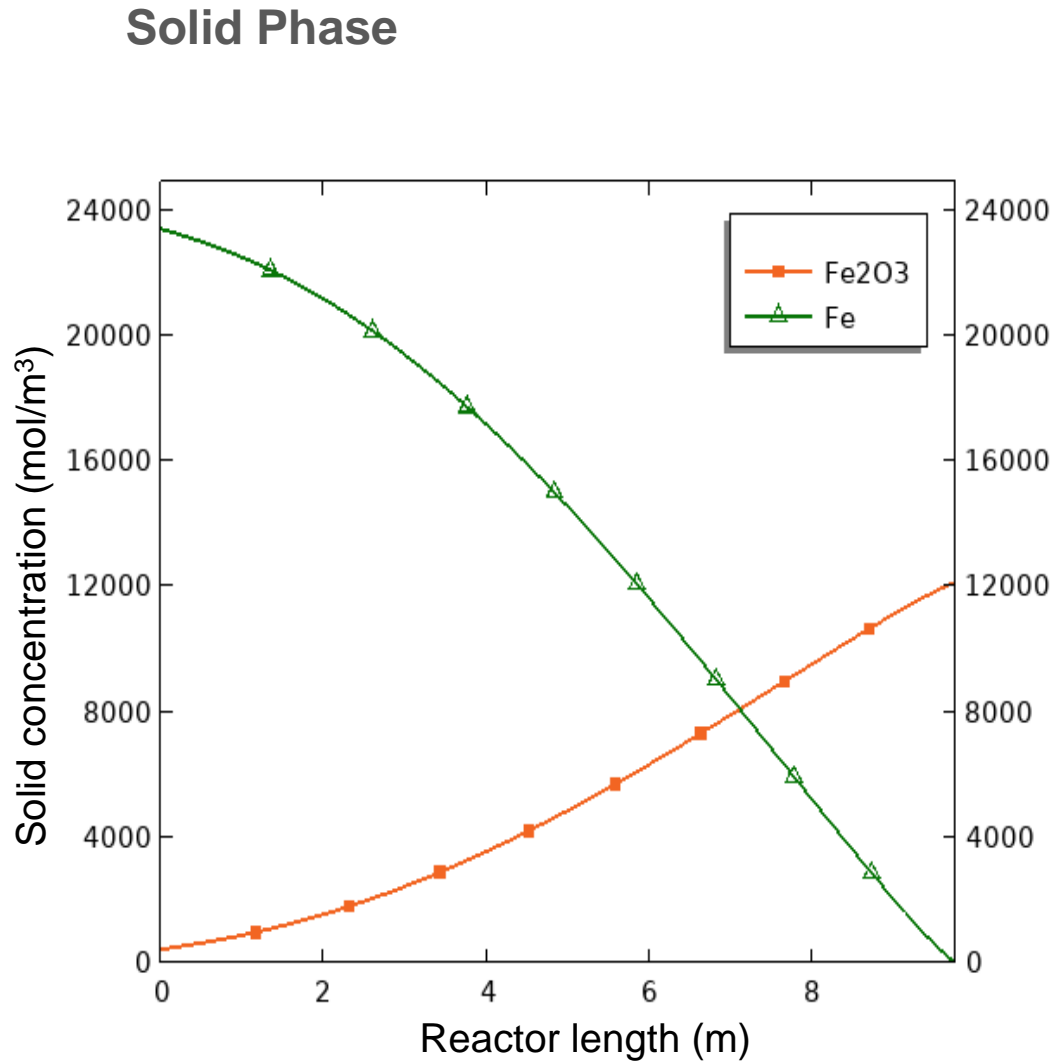
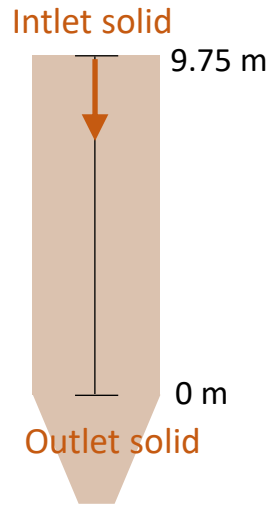
Pellet Scale



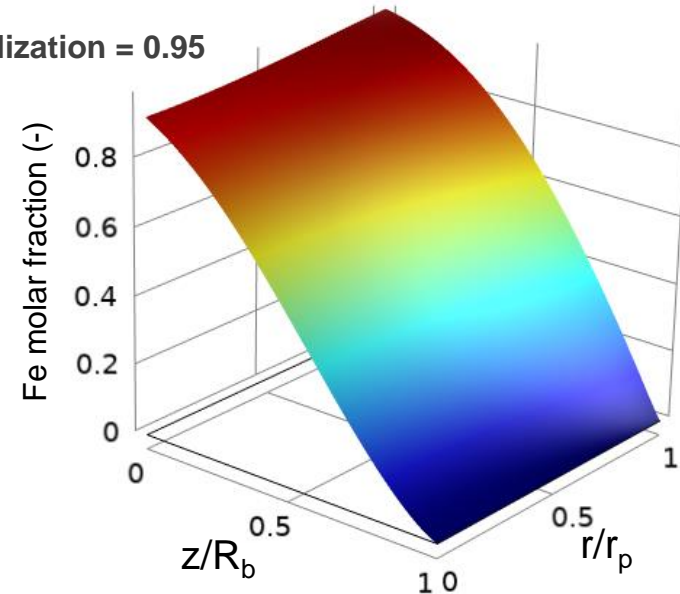
Gas Phase



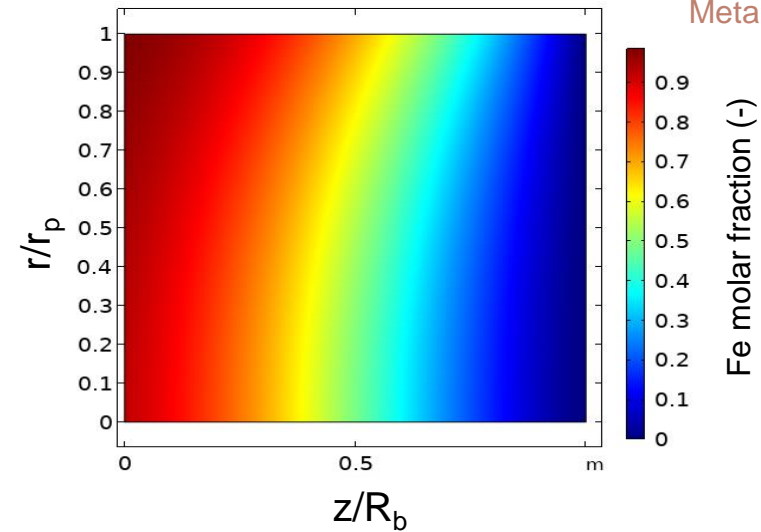
Reactor-Pellet Scale



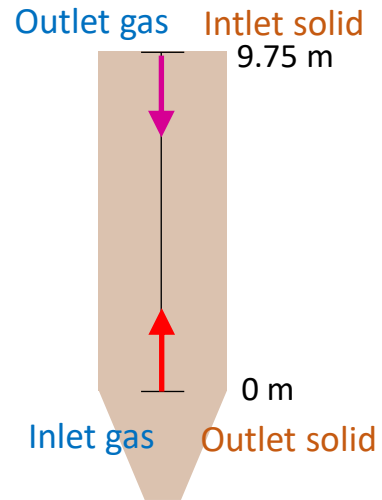
Metallization = 0.95



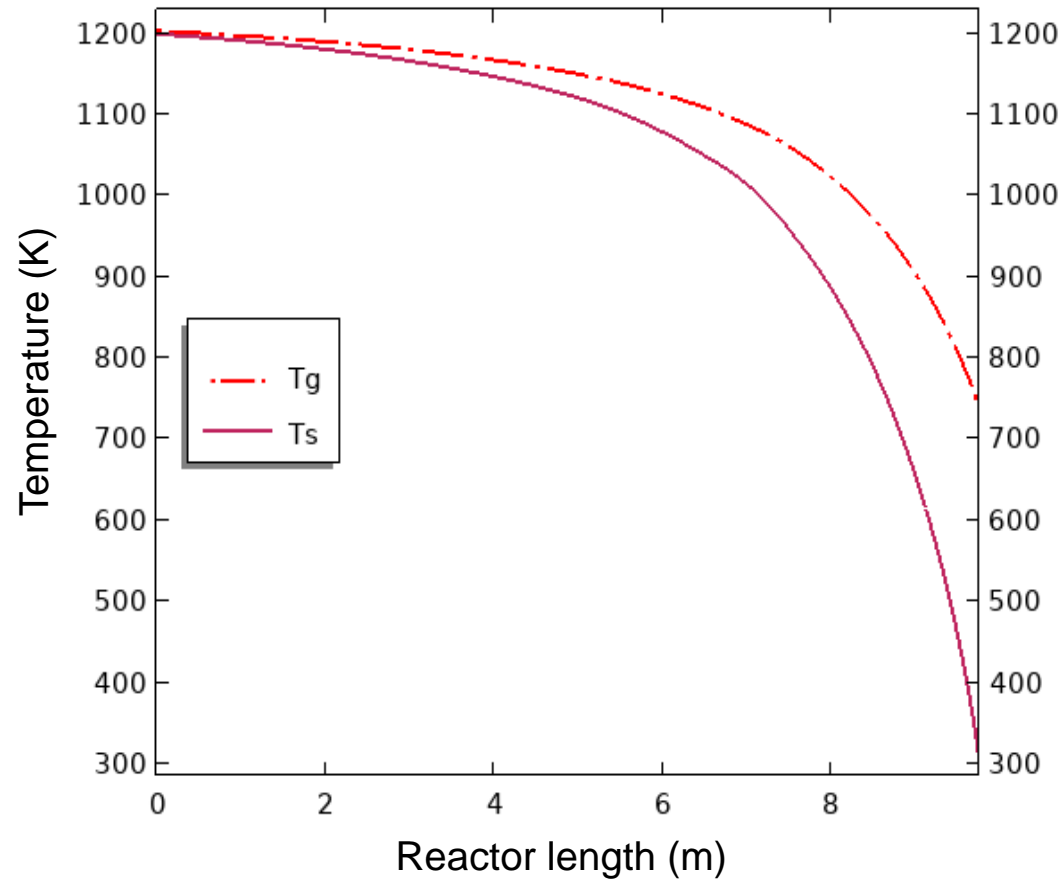
Gilmore Plant data
Metallization = 0.93



Reactor Scale



Temperature of the gas (T_g) and solid (T_s) along the reactor length



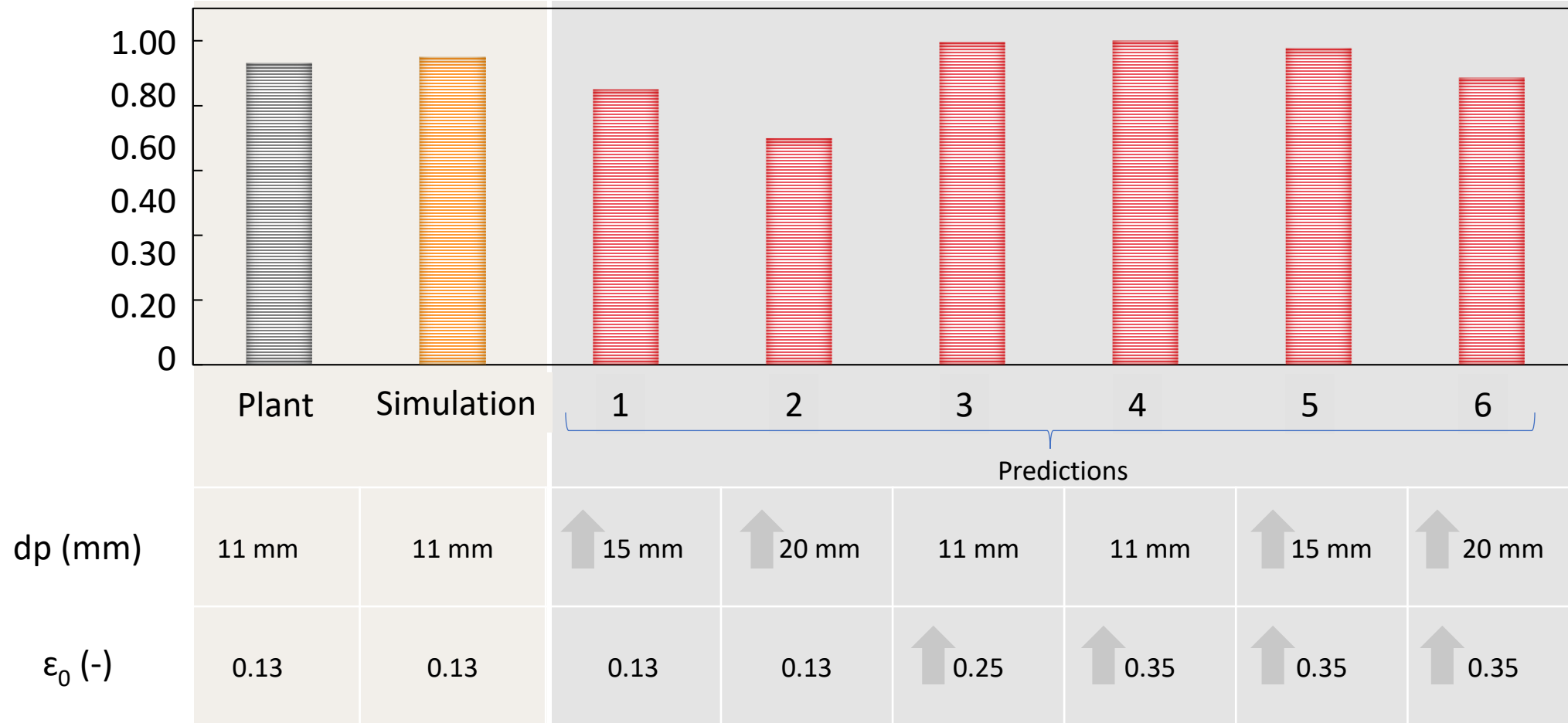
Pellet Scale

Isothermal pellet

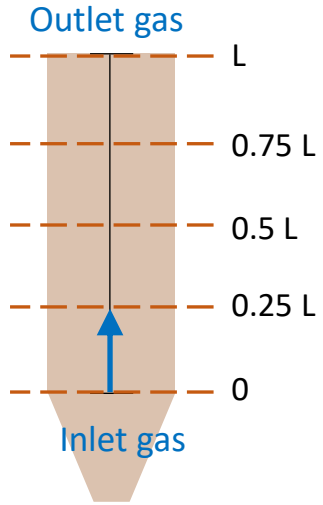
Biot number < 0.1

Reactor Scale

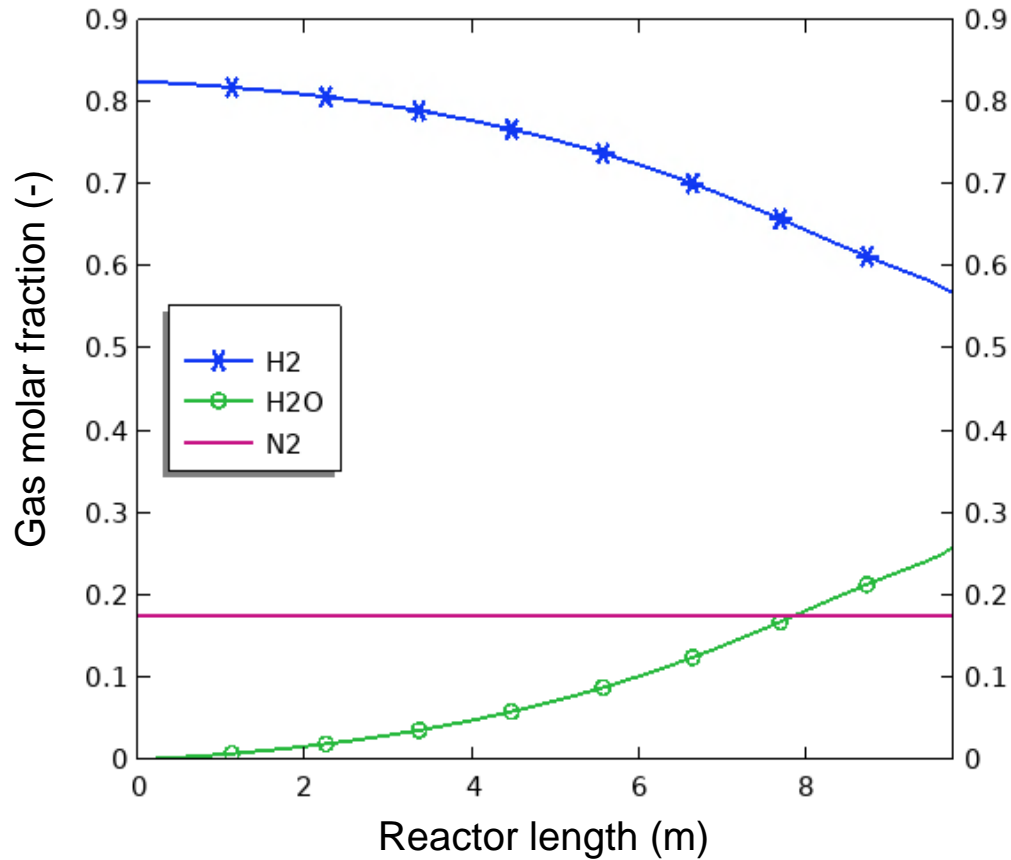
Sensitivity analysis of the structural parameters of the pellet



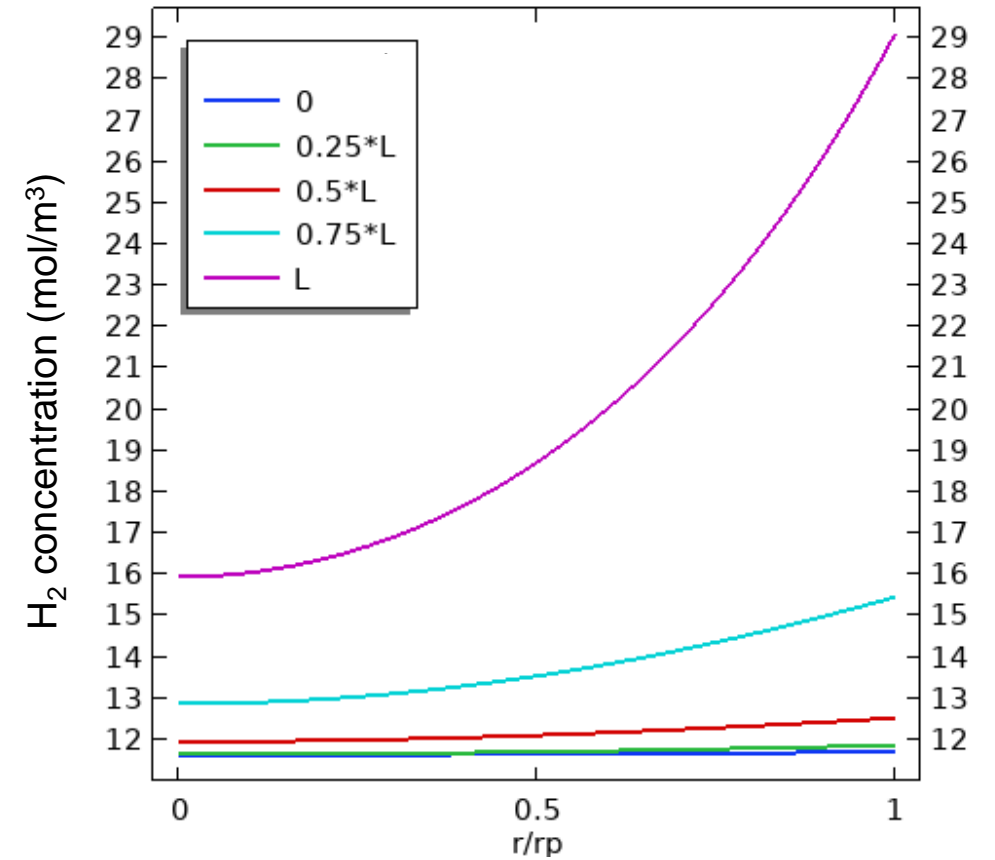
Reactor Scale for H-DR process



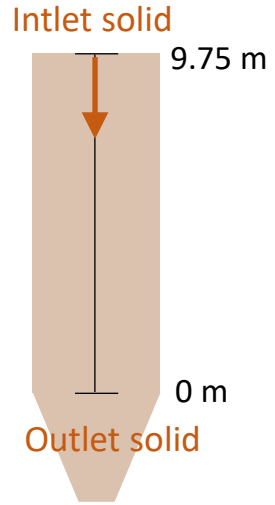
Gas phase – reactor scale



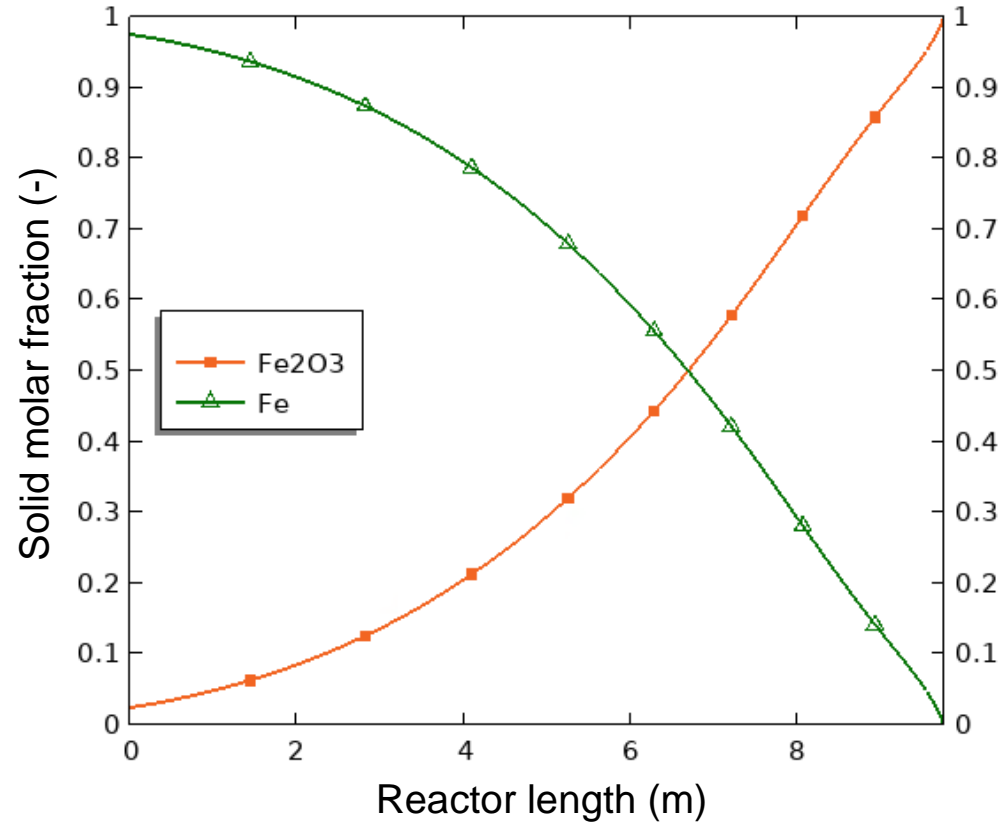
Gas phase – pellet scale



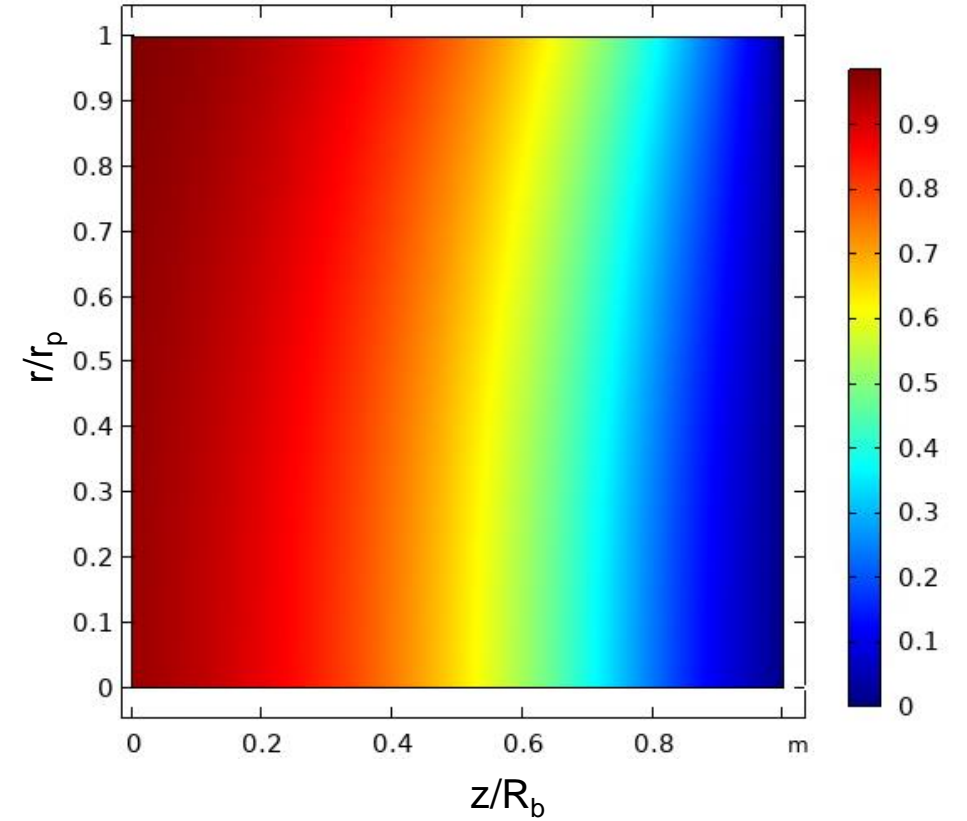
Reactor-Pellet Scale for H-DR process



Solid phase – reactor scale

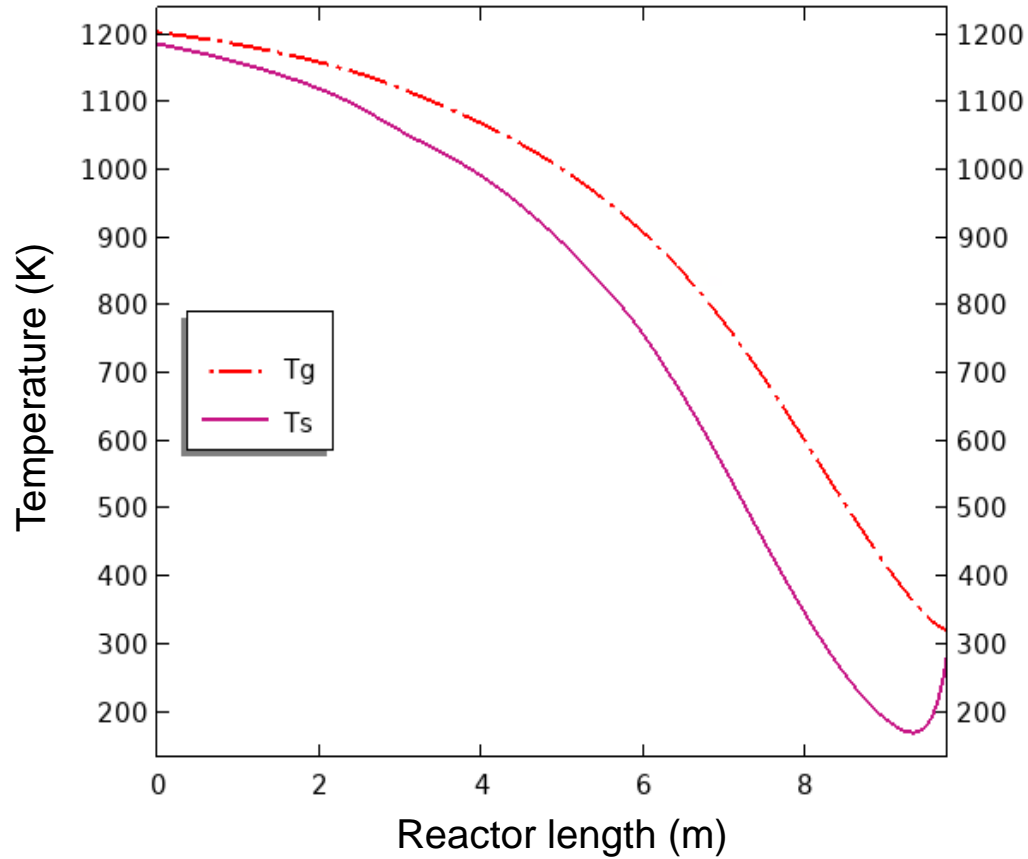
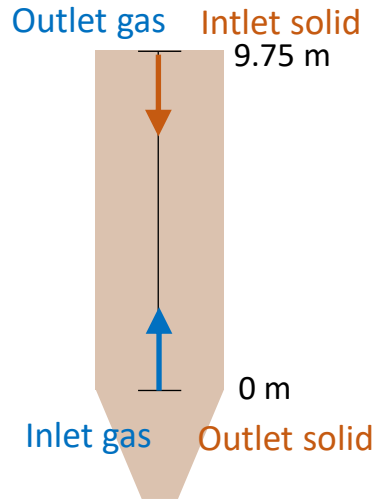


Solid phase – reactor-pellet scale



Reactor Scale for H-DR process

Temperature of the gas (T_g) and solid (T_s) along the reactor length



Pellet Scale

Isothermal pellet

Biot number < 0.1

Contents

01. Introduction

02. Literature Review

03. Objectives

04. Methodology

05. Results and Discussion

06. Conclusion



Conclusions

- ✓ Multiscale modelling shows **good agreement** with **industrial plant data**.
- ✓ **Structural pellet parameters** considerable **influence** the **reduction rate**.
- ✓ **Smaller** the pellet size, **higher** the reduction rate.
- ✓ **Greater** the pellet porosity, **higher** the reduction rate.
- ✓ Useful **predictions** for **H-DR**.

THANK YOU !

Patrícia Metolina

Chemical Engineer | Master of Engineering

PhD Student at Escola Politécnica da Universidade de São Paulo (Poli - USP)

pmetoli@gmail.com | [linkedin.com/in/patricia-metolina-7a784768](https://www.linkedin.com/in/patricia-metolina-7a784768)

